Aomori Public University Journal of Management & Economics Vol. 19, No. 2, 2014

# Aomori's Demographic Decline: Good News in Disguise?

## Hidetaka KAWANO\*

The National Institute of Population and Social Security Research reported this March that the demographic trend in Aomori Prefecture will be a decline by about 30 percent of the current population by the year 2040. The reaction of the general public to the report in Aomori is pessimistic about the future state of the economy. Our intuitive reaction, however, is encouraging. In this paper, we have estimated the economy-wide effects of the 30 percent decline of the current population in Aomori Prefecture, in the framework of a 13sector applied general equilibrium model. With the use of year 2000 Aomori input-output data, the major simulation results of the 30 percent decline of the current population lead to the following conclusions: 1) the Aomori prefecture will have an increasingly higher relative wage rate; 2) all the sectors, above all, the agricultural sector, will turn out to be increasingly more capital-intensive, and the economy-wide capital-labor ratio will increase; 3) labor productivity (relative marginal product of labor) will increase with the high capitallabor ratios in all sectors; 4) per capita income will increase, although the aggregate income will decline. These simulation results also imply that the demographic outflow of the population out of Aomori prefecture will result in an increase in the per capita income of the remaining population. "Voting with your feet" may benefit not only the people leaving the prefecture, but also the people who have decided to remain there.

JEL classification: C63; C68; D00; D58; F10; F11; F16; Q11; Q12; Q17; Q18

Keywords: General equilibrium; Factor intensities; Factor prices; Product prices; Welfare

#### 1. Introduction

The National Institute of Population and Research reported this March that the demographic trend in Aomori Prefecture will be a decline by about 30 percent of the current population by the year 2040 (National Institute of Population and Research, 2013). The reaction of the general public in Aomori to the report is pessimistic about the future state of the economy. Our reaction, however, is more optimistic than pessimistic by comparison.

In this paper, we have estimated the econ

omy-wide effects of the 30 percent decline of the current population in Aomori Prefecture, in the framework of a 13-sector applied general equilibrium model (AGE). With the use of year 2000 Aomori input-output data, the major simulation results of the 30 percent decline of the current population lead to the following conclusions: 1) the Aomori prefecture will have an increasingly higher relative wage rate by 50.1 %; 2) all the sectors, above all, the agricultural sector, will turn out to be increasingly more capital-intensive (the capital-labor ratio rises from 8.8 in 2000 to 13.2), and the economy-wide capital-labor ratio will

Aomori Public University Professor

increase by 42.9 %; 3) labor productivity (relative marginal product of labor) will increase with the high capitallabor ratios in all sectors by 50.1 %; 4) per capita income will increase by 0.9 %, although the aggregate income will decline by 29.4 %.

These simulation results also imply that the demographic outflow of the population out of Aomori prefecture will result in an increase in the per capita income of the remaining population. "Voting with your feet" may benefit not only the people leaving the prefecture, but also the people who have decided to remain there.

For the empirical characterization, calibration is achieved through the use of year 2000 Aomori's 13-sector input-output data (Kikaku Seisaku Tokei Bunsekika, 2005). The model closure assumes a small open economy with free capital inflow and outflow, so that the balance of payments is balanced. In this way, the original input-output data was used without modification.

A crucial step in the empirical characterization of an AGE is calibration, defined as "the requirement that the entire model specification be capable of generating a base-year equilibrium observation as a model solution" (Shoven and Whalley, 1992). An AGE model is a very powerful framework for analysis of policy reforms that could be instituted for Pareto improvements in the current state of the economy. An important development since Scarf (1967) has been the use of observed data, such as an input-output table, in developing an AGE model.

The solution procedure for coding the model follows Shoven and Whalley (1992) by reducing the dimensionality of the solution space to the number of factors of production in this general equilibrium structure. The solution algorithm used for calibration is a fixed-point algorithm originally developed by

Kimbell and Harrison (1986) and modified by Kawano (2003). In his recent paper (Kawano, 2006, 2013), seven alternative fixed point algorithms were compared. Among the seven alternatives, the modified Kimbell-Harrison approach was shown to be the best for an AGE modeling.

These experiments were programmed in C-language, and conducted on the GCC version 4.0.1 compiler (Apple Computer, Inc.). The verified reliability of the simulation results in double precision (1.0e-15). The converged equilibrium values in this benchmark model were obtained through 66 iterations over the entire model. In the full paper, Section 2 reviews the empirical structure of an AGE model. In Section 3, the calibration procedure is stated briefly. Section 4 reviews the major simulation results of the 30 percent decline of the current population in Aomori-prefecture. In section 5, policy implications are presented. The conclusion follows in section 6.

# 2 The Empirical Structure of the Model

#### 2.1 The Main Features of the Model

The model was kept very simple. The supply side of a theoretical general equilibrium model is made more empirically plausible by incorporating the Leontief type input-output accounting data.

An important step in building an empirical model is to incorporate flow of intermediate goods into the model structure. The flow of intermediate goods among different sectors is built into the model as part of production activity in the economy

The model is simple and has only 13 sectors, shown by subscript  $i \in I = \{0, ..., 12\}$ , and two final consumption commodities  $X_{i \in I}$ . The use of intermediate goods in production activities shows that total output  $Q_{i \in I}$  in sector

i will go partly to meet domestic household consumption demand  $X_{i\in I}$ , external sector consumption  $ES_{i\in I}$ , and also intermediate input demand  $q_{ij}$  for production of goods  $j\in J=\{0,...,12\}$ . The production activities of firms include intermediate goods  $Q_{j\in J}$  supplied through output markets. The usual primary factors of production are capital  $K_{i\in I}$  and labor  $L_{i\in I}$ . As in the Leontief system, intermediate inputs are required as a fixed proportion of the total output  $Q_{i\in I}$ . The input-

output coefficients  $a_{ij}$  are defined as:

$$a_{ij} \equiv \frac{q_{ij}}{Q_i}, \quad \forall \quad i \in I, j \in J,$$
 (1)

where

 $a_{ij}$  := input-output coefficient for commodity i used as an intermediate good to produce one unit of commodity j

 $q_{ij} :=$  amount of good i used as an intermediate input for production of good j ,

 $Q_j := \text{output in industry } j$ .

Table 1. Input-Output Accounting Table Flows (Yen Trillion)

	Inputs to	Input to			Domestic	External	Total
	industry 0	industry 1			consumption	sector	output
Industry 0	$q_{00} = a_{00} \cdot Q_0$	$q_{01} = a_{01} \cdot Q_1$	•••	$q_{012}$	$X_0$	$ES_0$	$Q_0$
Industry 1	$q_{10} = a_{10} \cdot Q_0$	$q_{11}=a_{11}\cdot Q_1$	•••	$q_{112}$	$X_1$	$ES_1$	$Q_1$
•••		•••	•••				
Industry 12	$q_{120} = a_{120} \cdot Q_0$	$q_{121} = a_{121} \cdot Q_1$	•••	$q_{1212}$	$X_{12}$	$ES_{12}$	$Q_1$
Capital	$K_0$	$K_1$		$K_{12}$	$ar{K}$		
Labor	$L_0$	$L_1$	•••	$L_{12}$	$ar{L}$		

Note: Capital is broadly defined as gross value added without labor income.

The input-output table in Table 1 can be looked at in both rows and columns. Here, the table is interpreted in rows.

In row 0 in the table, the value of the domestic production in sector 0 is  $Q_0$  trillion yen. Sales value of  $q_{00}$  trillion yen goes to its own sector 0, the other  $q_{01}$  trillion yen through  $q_{012}$  trillion yen go to sector 1 through sector 12 respectively.  $X_0$  trillion yen through  $X_{12}$  trillion yen for domestic consumptions for sectors 0 through 12, and the remaining  $ES_0$  through  $ES_{12}$  trillion yen worth of net import/export from external sector.

In rows 1-12, the table is interpreted in the same way as row 0.

In row 13, the total endowment of capital is  $\bar{K}$  trillion yen, of which  $K_0$  trillion yen worth of capital is used in sector 0,  $K_1$  trillion yen worth of capital is used in sector 1,

and in the same way  $K_2 - K_{12}$  trillion yen worth of capital are used in sectors 2 though 12, respectively.

In row 14, the total endowment of labor is  $\bar{L}$  trillion yen, of which  $L_0$  trillion yen worth of labor is used in sector 0,  $L_1$  trillion yen worth of capital is used in sector 1, and in the same way  $L_2-L_{12}$  trillion yen worth of labor are used in sectors 2 though 12, respectively.

#### 2.2 The Demand Side of the Model

The level of disposable income for a representative consumer is determined by factor endowments, factor prices, and external finance. The disposable income Y is:

$$Y = w\bar{L} + r\bar{K} + EF,\tag{2}$$

where

w := wage rate,

r := rental rate,

 $\bar{L} := labor endowment,$ 

 $\bar{K} := \text{capital endowment},$ 

EF:= external finance.

We assume a simple Cobb-Douglas utility function U(.) as a representation of consumer preference.

The function is:

$$U(X_0, ..., X_{12}) = \prod_{i=0}^{12} X_i^{\theta_i},$$

$$\therefore \quad 0 < \theta_i < 1, \quad \sum_{i=0}^{12} \theta_i = 1, \quad \forall i \in I. \quad (3)$$

The final demand for commodities  $X_{i \in I}$  is derived by the utility maximization for a representative consumer as:

$$X_i = \frac{\theta_i Y}{p_i}, \quad \forall i \in I, \tag{4}$$

where

 $\theta_{i \in I} :=$  share parameter in utility function,

 $p_i$ := price of commodity.

## 2.3 The Production Side of the Model

The production function with intermediate inputs is modeled as:

$$Q_{j} = min\left(\frac{q_{0j}}{a_{0j}}, \frac{q_{1j}}{a_{1j}}, \dots, \frac{q_{12j}}{a_{12j}}, VA_{j}\right),$$

$$\forall j \in J. \tag{5}$$

where

 $Q_j := \text{commodity } j \in J \text{ produced},$ 

 $VA_i$ := value-added component of production function  $j \in J$ .

The value-added component  $VA_{j\in J}$  of production function  $j \in J$  is modeled as Cobballows Douglas which the substitution possibility between primary factors: capital  $K_i$ and labor  $L_j$ . The value-added component  $VA_j$ is specified as:

$$VA_{j} \equiv \Phi_{i}K_{i}^{\alpha_{i}}L_{i}^{1-\alpha_{i}}, : 0 < \alpha_{i} < 1,$$

$$\forall i \in I, \quad (6)$$

where

 $\alpha_{i \in I}$ := factor share parameter in valueadded component of production function (or value added output elasticity of capital),

 $\Phi_{i \in I}$ := shift parameter in value-added component of production function.

 $K_{i \in I}$ := capital employed in sector  $i \in I$ ,

 $L_{i \in I}$ := labor employed in sector  $i \in I$ .

The conditional factor demand functions can be derived by assuming no intermediate goods are needed in the model, since a fixed proportion of the total output  $Q_i$  does not affect the first order conditions of the producers' cost minimization.

1) The per unit capital demand function is:

$$k_{i} = \frac{1}{\Phi_{i}} \left( \frac{\alpha_{i}}{1 - \alpha_{i}} \right)^{1 - \alpha_{i}} \left( \frac{w}{r} \right)^{1 - \alpha_{i}}, \qquad (7)$$

$$\forall i \in I.$$

2) The per unit labor demand function is:

$$l_i = \frac{1}{\Phi_i} \left( \frac{\alpha_i}{1 - \alpha_i} \right)^{-\alpha_i} \left( \frac{w}{r} \right)^{-\alpha_i}, \quad \forall i \in I. \quad (8)$$

#### 2.4 Zero Profit Conditions

Perfectly competitive behavior in producers will imply zero profit conditions. Zero profit conditions for the two producers with intermediate goods are modeled as: For the producer in sector  $i \in I$ ,

$$p_i = \sum_{i \in I} a_{ij} p_j + rk_i + wl_i, \qquad \forall i \in I, \qquad (9)$$

where

 $k_i :=$  capital employed for per unit production of commodity  $i \in I$ ,

 $l_i := labor employed for per unit produc$ tion of commodity  $i \in I$ .

Rewrite equations (9) in matrix as:

$$(I - A^T)P = W. (10)$$

Solve for P as:

$$P = (I - A^T)^{-1}W. (11)$$

## 2.5 Market Clearing Conditions

The total output  $Q_{i \in I}$  of commodity in sector  $i \in I$  is met by the total intermediate input demand  $\sum_{j \in J} q_{ij}$ , domestic consumption demand  $X_{i \in I}$ , and external consumption demand  $ES_{i \in I}$  as:

$$Q_i = \sum_{j \in J} q_{ij} + X_i + ES_i, \quad \forall i \in I.$$
 (12)

By equation (1),  $q_{ij} = a_{ij}Q_j$ . Rewrite equation (12) as:

$$Q_i = \sum_{j \in J} a_{ij} Q_j + X_i + ES_i, \quad \forall i \in I.$$
 (13)

Further rewrite equation (13) in matrix as:

$$(I - A)Q = X + ES. (14)$$

Solve for Q as:

$$Q = (I - A)^{-1}(X + ES). (15)$$

#### 3 Calibration Procedure

Here, we calibrated the general equilibrium model to be consistent with an actual data set. In other words, choose the model parameters to replicate the real data at hand. The calibration procedure is as follows:

**Step 1**: Read information from the year 2000 Aomori 13-sector input-output data file. The program uses the input-output data to calibrate parameters. The calibrated parameters are: 1) consumptionshare (preference elasticity) parameters  $\theta_{i \in I}$ , 2) factor-share (output elasticity) parameters  $\alpha_{i \in I}$ , 3) input-output coefficients  $a_{i \in I, j \in J}$ , and 4) shift parameters in production  $\Phi_{i \in I}$ . These parameters are computed in double precision.

**Step 2**: Generate a micro-consistent data set summarized in the social accounting matrix for the year 2000 shown in the output file in Appendix. Its zero-sum row shows that all

goods and factor markets are cleared. Its zerosum column shows that income equals expenditure in each sector.

The generated data set shows micro-consistent financial flows in all sectors of the economy. In other words, the data is consistent with the underlying general equilibrium structure of the model.

**Step 3**: Conduct the replication check to see if the calibrated solutions in the model are error-free in building and coding the model. The generated data is identical to the original input-output table data in the output file in Appendix. The replication check has passed, so the data is considered as an appropriate benchmark for comparative static experiments.

#### 4 Simulation Results

We have estimated the economy-wide effects of the 30 percent decline of the current population in Aomori Prefecture, in the framework of a 13-sector applied general equilibrium model. With the use of year 2000 Aomori input-output data, the major simulation results lead to the following conclusions: 1) the Aomori prefecture will have an increasingly higher relative wage rate by 50.1%, which means that active productive labor become extremely scarce and expensive if the effect of the declining demographic trend is combined with the aging population; 2) all the sectors, above all, the agricultural sector, will turn out to be increasingly more capitalintensive (from 8.8 in 2000 to 13.2), and the economy-wide capital-labor ratio will increase by 42.9 %, which means that expensive and scarce labor is substituted for relatively inexpensive capital in the process of production in all sectors; 3) labor productivity (relative marginal product of labor) will increase with the high capital-labor ratios in all sectors by 50.1 %, which means that increasing the labor productivity with more employment of capital per unit of labor will make it possible for the wage rate to go up; 4) per capita income will increase by 0.9% ( $\frac{1}{2}600,000$  through  $\frac{1}{2}700,000$  by CV and EV measures), although the aggregate income will decline by  $\frac{1}{2}9.4\%$ .

## 5 Policy Implications

In this rapid demographic outflow of the Aomori prefecture population, the local government must first consider the characteristic features that both private companies and Aomori-prefecture herself need to survive: a flexible labor market. The central government of Japan must help devise "the more flexible labor market" which would allow local governments all over Japan to act on their own initiatives to adjust to the constantly changing economic environment. If that happens, then the above simulation scenario will come true.

Once this implied flexible labor market is instituted nationwide, then it will enable workers to move easily from one prefecture to another. With this government initiative, private firms can hire and fire employees with relative ease, which is crucial for giving renewed vitality to the whole economy of Japan, and especially Aomori prefecture located at the northern tip of Japan.

Domestic local economies need to adjust themselves to the changing environment. One loses one's job in one place one day, and the following day they find another job in another place. In a world of fast changing environments, one should be prepared to move from one place to another, which is exactly what "Voting with your feet" means. The Aomori local government should not

discourage people from going out of the prefecture, by all means. At the same time, private firms

have more incentive to hire employees, because they can easily fire employees if they engage actively in unraveling any mismatch between employees and firms.

The ideal environment of a thriving economy in which the most private firm operates must be highly competitive, where "Schump eterian Creative Destruction" is at work in order to make the economic pie larger before distributional policies are implemented. If more flexible local labor markets are instituted nationwide by the central government, a local market like Aomori will be bound to thrive.

If, on the contrary, the labor markets in Aomori remain stagnant, and do not strive for more flexibility, this stagnation will continue to be reflected in the economy for a long time, much of which Japan has experienced for more than two decades. What is crucial for the thriving economy is the functioning of both factor and product markets. Private firms and even the central government as well as many local governments at all levels must stand on their own. Any form of governmentsubsidized organizations, cartels, and monopolies need to be eliminated or dismantled, which is also of paramount importance to the elimination of rent-seeking and the reduction of the enormous public debts accumulated over the years.

### 6 Conclusion

In this paper, we have estimated the economy-wide effects of the 30 percent decline of the current population in Aomori Prefecture, in the framework of a multi-sector AGE model. The simulation results show that the

pessimistic reaction of general public in Aomori to the government agency report of a decline by about 30 percent of the current population are unwarranted. The key policy question should be how more competitive and flexible product-factor markets, especially the labor market, can be facilitated to improve the future prospect of the economy in Aomori. (Received: December 2, 2013, Accepted: January 14, 2014)

#### References

Kawano, Hidetaka (2003) "A Simultaneous Multi-Factor Price Revision for Solving a Numerical General Equilibrium Model," *Aomori Public College Journal of Managemet & Economics*, Vol. 8, No. 2, pp. 2?27.

ternative Fixed Point Algorithms for Applied General Equilibrium Modeling,"

Aomori Public College Journal of Management & Economics, Vol. 11, No. 2, pp. 15-21.

——— (2013) "Comparison of Seven

Alternative Algorithms for Applied General Equilibrium Modeling," *Aomori Public College Journal of Management & Economics*, Vol. 18, No. 2, pp. 23-31.

Kikaku Seisaku Tokei Bunsekika (2005) "Year 2000 Aomori's 13-input-output data." Available at: http://www6.pref.aomori.lg.jp/tokei/(accessed September 4, 2013).

Kimbell, Larry J. and Glenn. W. Harrison (1986) "On the solution of general equilibrium models," *Economic Modelling*, Vol. 3, pp. 197-212, July.

National Institute of Population and Social Security Research (2013) "Nihon no Tiikibetu Syourai Suikei Jinko (The future trend of Regional Population Estimates in Japan)." Available at:http://http://www.ipss.go.jp/pp-icyoson/j/shicyosonl3/t-page.asp.

Scarf, Hubert E. (1967) On the Computation of Equilibrium Prices. In Ten Economic Essays in the Tradition of Irving Fisher, New York: Wiley.

Shoven, John B. and John Whalley (1992)

Applying General Equilibrium, New York:
Cambridge University Press.

```
====The output file=====PART II==
   PROGRAM: aomori_13sec_2000_5-2.c
DATE: September 15,2013
     NAME: Hidetaka Kawano
   NAME: Hidetaka Rawaro
Data: Ammori 13 mector Input Output in 2000
Input File: ammori 13sec 2000 2 txt
TOPICS: Comparative statio of Decreasing 30 percent of labor endowment in 2000
 /// 0. Defining the sectors in Aomori ///
Sector 0: Agriculture
Sector 1: Forestry
Sector 2: Fishery
                            Sector
                                                                        3: Mining
4: Manufacturing
5: Construction
                            Sector
                            Sector
                           Sector 5: Construction
Sector 6: Power_gas_water
Sector 7: Commerce
Sector 8: Finance_insurance_real estate
Sector 9: Transport_communication_broadcast
Sector 10: Public service
Sector 11: Service
Sector 12: Miscellaneous
/// 1. Calibrated consumption share parameters: theta[]///
(1- 1) theta[0]= 0.007157977136202
(1- 2) theta[1]= 0.03314296199454
(1- 3) theta[1]= 0.03314296199454
(1- 3) theta[2]= 0.002289746213475
(1- 4) theta[3]= 0.00056230943444
(1- 5) theta[4]= 0.167823470351865
(1- 7) theta[4]= 0.167823470351865
(1- 7) theta[6]= 0.013308791486043
(1- 8) theta[7]= 0.096772898756926
(1- 9) theta[7]= 0.096772898756926
(1- 9) theta[8]= 0.112004825502805
(1-10) theta[9]= 0.41321604742340
(1-11) theta[10]= 0.102576893956458
(1-12) theta[11]= 0.263862777261094
(1-13) theta[12]= 0.000061410109288
                                           sum theta= 1.0000000000000000
/// 2. Calibrated production share parameters: alpha[] ///
Capital share
(2- 1) alpha[ 0]= 0.897885397003031
(2- 2) alpha[ 1]= 0.672586015538291
(2- 3) alpha[ 2]= 0.712575696882584
1-alpha[ 2]= 0.32743984461709
(2- 3) alpha[ 3]= 0.616372170071784
(2- 4) alpha[ 3]= 0.616372170071784
(2- 5) alpha[ 4]= 0.506487425924551
1-alpha[ 3]= 0.383627829928216
(2- 5) alpha[ 5]= 0.270364564033863
(2- 7) alpha[ 6]= 0.6588591823074737
1-alpha[ 7]= 0.395456569188370
(2- 9) alpha[ 7]= 0.305465696188470
(2- 9) alpha[ 8]= 0.8284035589334967
1-alpha[ 7]= 0.658720525851015
(2- 10] alpha[ 1]= 0.26797467148998
(2- 10] alpha[ 1]= 0.26797467148998
(2- 11) alpha[ 1]= 0.26797467148998
(2- 12) alpha[ 1]= 0.26797467148998
(2- 13) alpha[ 1]= 0.2789854549404710
1-alpha[ 1]= 0.2789858788318
(2- 13) alpha[ 1]= 0.2789854549404710
   /// 3. Calibrated input-output coefficients: a[][] ///
   (6) (1) (2) (3) (4) (5) (6) (7) (8) (9) (10) (11) (12) (0) 0.108382 0.002330 0.000000 0.000000 0.0057905 0.002168 0.000000 0.000111 0.000000 0.000013 0.000090 0.005495 0.000000
 0.458568 \quad 0.300155 \quad 0.350947 \quad 0.524589 \quad 0.574332 \quad 0.523340 \quad 0.444602 \quad 0.284758 \quad 0.195441 \quad 0.358182 \quad 0.376630 \quad 0.348648 \quad 0.351463 \quad 0.541432 \quad 0.699845 \quad 0.649053 \quad 0.475411 \quad 0.425668 \quad 0.476660 \quad 0.444602 \quad 0.284758 \quad 0.195441 \quad 0.358182 \quad 0.376630 \quad 0.348648 \quad 0.351463 \quad 0.351463 \quad 0.348648 \quad 0.351464 \quad 0.3514644
/// 4. Calibrated shift parameters in production: phi[] ///
(4-1) phi[ 0]= 2.568295421633889
(4-2) phi[ 1]= 2.689160356285795
(4-3) phi[ 2]= 2.806859270201006
(4-4) phi[ 3]= 4.093446351692414
(4-5) phi[ 4]= 4.698103991893418
(4-6) phi[ 5]= 3.760582651801370
(4-7) phi[ 6]= 3.21349088057585
(4-8) phi[ 7]= 2.587155738418556
(4-9) phi[ 8]= 1.965742594948587
(4-10) phi[ 9]= 3.002038572979871
(4-11) phi[ 10]= 1.904343957452518
(4-12) phi[ 1]= 2.754239457654359
(4-13) phi[12]= 2.581508842665020
 /// 5. Factor endowments ///
(5- 1) Capital kbar= 1.979455000000000
(5- 2) Labor lbar= 1.904961800000000
                                                                                                                                                                                                                                                                            NOTE: Up by -30.000000 percent !
   /// 6. Numeraire ///
(6- 1) Wage rate w= 1.000000000000000
/// 7. Commodity prices: p[1]// (7-1) p[0] = 0, 74266894677842 (7-2) p[1] = 0, 71099503604980 (7-3) p[2] = 0, 71099503604980 (7-4) p[3] = 0, 81098039791425 (7-4) p[3] = 0, 802048399791425 (7-5) p[4] = 0, 813406991534969 (7-6) p[5] = 0, 860976033497551 (7-7) p[6] = 0, 790533900811243 (7-8) p[7] = 0, 860555111984423 (7-8) p[7] = 0, 860555111984423 (7-10) p[9] = 0, 850556868576174 (7-11) p[10] = 0, 927887428721988 (7-12) p[11] = 0, 87151622682594 (7-13) p[12] = 0, 760051747406557
                                                                                                                                                                                                                 NOTE: Up by -25.733411 percent
NOTE: Up by -22.890050 percent
NOTE: Up by -22.756848 percent
NOTE: Up by -19.795160 percent
NOTE: Up by -19.795160 percent
NOTE: Up by -18.659391 percent
NOTE: Up by -13.902397 percent
NOTE: Up by -20.946610 percent
NOTE: Up by -26.647879 percent
NOTE: Up by -14.940313 percent
NOTE: Up by -14.940313 percent
NOTE: Up by -1.294787 percent
NOTE: Up by -12.847888 percent
NOTE: Up by -23.994825 percent
```

```
/// 8. Factor prices ///
(8- 1) w = 1.000000000000000
(8- 2) r = 0.666036552337701
(8- 3) w/r= 1.501419098531652
(8- 4) r/w= 0.666036552337701
                                                                                                                                                                                                                  NOTE: Up by 50.141910 percent
NOTE: Up by -33.396345 percent
 /// 9. Income & expenditure ///
(9- 1) Expenditure on X[ 0]: p[ 0]*X[ 0] = 0.027319090307530
(9- 2) Expenditure on X[ 1]: p[ 1]*X[ 1] = 0.012643321332150
(9- 3) Expenditure on X[ 2]: p[ 2]*X[ 2] = 0.008739030929684
(9- 4) Expenditure on X[ 3]: p[ 3]*X[ 3] = 0.00216161663432
(9- 5) Expenditure on X[ 3]: p[ 3]*X[ 3] = 0.00216116663432
(9- 5) Expenditure on X[ 4]: p[ 4]*X[ 4] = 0.60513996486182
(9- 6) Expenditure on X[ 5]: p[ 5]*X[ 5] = 0.723050151435135
(9- 7) Expenditure on X[ 6]: p[ 6]*X[ 6] = 0.050794249488788
(9- 9) Expenditure on X[ 7]: p[ 7]*X[ 7] = 0.369424333897980
(9- 9) Expenditure on X[ 8]: p[ 8]*X[ 8] = 0.427476909267366
(9-10) Expenditure on X[ 9]: p[ 9]*X[ 9] = 0.15707775552769
(9-11) Expenditure on X[ 1]: p[ 1]*X[ 1] = 1.00757008373730
(9-13) Expenditure on X[ 1]: p[ 1]*X[ 1] = 1.00757008373730
(9-13) Expenditure on X[ 1]: p[ 1]*X[ 1] = 1.00757008373730
                                   9. Income & expenditure
   (9-14) Total expenditure = 3.816593681105842
(9-15) Factor income y=r*kbar+w*lbar+EF = 3.816593681105841
(9-16) Per capita-income y/lbar = 2.003501425123507
                                                                                                                                                                                                                                                                                                                                                                                         NOTE: Up by -29.404387 percent
                                                                                                                                                                                                                                                                                                                                                                                NOTE: Up by
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            0.850876 percent !
/// 10. Factor markets ///
--- Sectoral capital use --
(10-1) k[ 0] = 0.137138919452980
(10-2) k[ 1] = 0.017002022907013
(10-3) k[ 2] = 0.027089747752236
(10-4) k[ 3] = 0.01252109452240
(10-5) k[ 4] = 0.308236042625237
(10-6) k[ 5] = 0.157088718181208
(10-7) k[ 6] = 0.064991333171514
(10-8) k[ 7] = 0.218893238171514
(10-9) k[ 8] = 0.567017760742805
(10-10) k[ 9] = 0.130624407964281
(10-11) k[10] = 0.0160717828155078
(10-12) k[11] = 0.306592812411246
(10-13) k[12] = 0.016396101023717
                                                                                                                                                                                                                      NOTE: Up by -6.084671 percent !
NOTE: Up by -0.200512 percent !
NOTE: Up by -0.420463 percent !
NOTE: Up by -6.441885 percent !
NOTE: Up by -7.787199 percent !
NOTE: Up by -7.787199 percent !
NOTE: Up by -9.713794 percent !
NOTE: Up by -9.713798 percent !
NOTE: Up by -1.504697 percent !
NOTE: Up by 6.672226 percent !
NOTE: Up by 4.12954 percent !
NOTE: Up by 4.12954 percent !
NOTE: Up by 4.12954 percent !
   --- Total capital use and endowmen
(10-14) Capital use= 1.97945499999999
(10-15) kbar= 1.979455000000000
 --- Sectoral labor use --- (10-16) (10-16) (10) --- (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (10-16) (1
                                                        Sectoral labor use
                                                                                                                                                                                                                      NOTE: Up by -37.448958 percent !
NOTE: Up by -33.262796 percent !
NOTE: Up by -33.662796 percent !
NOTE: Up by -37.686876 percent !
NOTE: Up by -37.686876 percent !
NOTE: Up by -26.463104 percent !
NOTE: Up by -26.463104 percent !
NOTE: Up by -26.926261 percent !
NOTE: Up by -26.926261 percent !
NOTE: Up by -34.938528 percent !
NOTE: Up by -28.952398 percent !
NOTE: Up by -25.144092 percent !
NOTE: Up by -30.645911 percent !
NOTE: Up by -30.645911 percent !
NOTE: Up by -40.185827 percent !
                                   --- Total labor use & endowment ---
   (10-29) labor use= 1.904961800000001
(10-30) lbar= 1.904961800000000
     --- Excess demand for capital & labor --- (10-31) rho_k= -0.00000000000001 (10-32) rho_l= 0.00000000000001
 Sectoral capital/labor ratio
   --- Economy-wide capital/labor ratio --- (10-46) kbar/lbar= 1.039104826144020 NOTE:
                                                                                                                                                                                                                                         NOTE: Up by 42.857143 percent !
/// 11. Commodity markets ///
--- Domestic Output ---
(11- 1) Per capita O[ 0]= 0.142064717600135
(11- 2) Per capita O[ 1]= 0.01659973988313
(11- 3) Per capita O[ 2]= 0.027357497353127
(11- 4) Per capita O[ 3]= 0.019209424701589
(11- 5) Per capita O[ 4]= 0.614117881725627
(11- 6) Per capita O[ 6]= 0.081137526165206
(11- 8) Per capita O[ 6]= 0.081137526165206
(11- 8) Per capita O[ 7]= 0.396429077894564
(11- 9) Per capita O[ 9]= 0.226509217185184
(11-11) Per capita O[ 1]= 0.62859127185184
(11-11) Per capita O[ 1]= 0.684591990441638
(11-13) Per capita O[ 1]= 0.684591990441638
(11-13) Per capita O[ 1]= 0.015554188973970
                                                                                                                                                                                                                                                                                NOTE: Up by 28.710808 percent !
NOTE: Up by 25.309126 percent !
NOTE: Up by 13.862267 percent !
NOTE: Up by 14.359531 percent !
NOTE: Up by 7.792179 percent !
                                                                                                                                                                                                                                                                                                                                                                      7.792179 percent
17.253854 percent
                                                                                                                                                                                                                                                                                        NOTE: Up by
                                                                                                                                                                                                                                                                                      NOTE: Up by
                                                                                                                                                                                                                                                                                                                                                                      12.444202 percent
                                                                                                                                                                                                                                                                                                                                                                    18.189414 percent
                                                                                                                                                                                                                                                                                      NOTE: Up by
                                                                                                                                                                                                                                                                                                                                                                    31.229168 percent
                                                                                                                                                                                                                                                                                    NOTE: Up by 17.749227 percent
NOTE: Up by 8.740281 percent
NOTE: Up by 10.474023 percent
NOTE: Up by 17.749227 percent
   --- Total value of domestic output --- (11-14) Total = 5.303245405547834
   --- Domestic demand---
(11-15) per capita X ( 0) = 0.019310187120643
(11-16) per capita X ( 1) = 0.008611336315917
(11-17) per capita X ( 2) = 0.00593050473433
(11-18) per capita X ( 3) = 0.00140463811605
(11-20) per capita X ( 4) = 0.413366171606399
(11-20) per capita X ( 5) = 0.440850246807970
                                                                                                                                                                                                                                                                                           NOTE: Up by 35.795755 percent !
                                                                                                                                                                                                                                                                                         NOTE: Up by 30.788407 percent !
NOTE: Up by 30.562869 percent !
NOTE: Up by 25.741633 percent !
NOTE: Up by 23.985887 percent !
NOTE: Up by 17.135520 percent !
```

```
(11-21) per capita X[ 6]= 0.033729334923647
(11-22) per capita X[ 7]= 0.224519127826473
(11-32) per capita X[ 8]= 0.305924116202476
(11-24) per capita X[ 9]= 0.097329177955062
(11-24) per capita X[ 10]= 0.221491522193137
(11-26) per capita X[ 11]= 0.606582139238766
(11-27) per capita X[ 11]= 0.00016374735601
                                                                                                                       NOTE: Up by
NOTE: Up by
NOTE: Up by
                                                                                                                                                        16.785685 percent
37.488698 percent
18.564833 percent
                                                                                                                        NOTE: Up by
                                                                                                                       NOTE: Up by
NOTE: Up by
NOTE: Up by
                                                                                                                                                            8.692211 percent
                                                                                                                                                         15.718157
                                                                                                                                                         32.689486 percent
 --- Total value of domestic demand --- (11-28) Total = 3.816593681105842
--- Total external sector demand --- (11-42) Total ES Value = -0.593242497398216
                  - Total external finance
 (11-43)
                                                  EF = 0.593242497398216
  /// 12. Individual Welfare (utility) level ///
 (12-1) u_autarky = 0.000000635496054
 (12-2) u_old = 0.00000531985690
(12-3) u_new = 0.00000635496054
(12-3) u_individual = 0.00000635496054
(12-4) y_old = 0.000003663463728
(12-5) y_new = 0.000003694635249
 (12-6) individual_cv=((u_new-u_old)/u_new)*y_new=601786.645951796090230
(12-7) individual_ev=((u_new-u_old)/u_old)*y_old=712813.277325085597113
 /// 13. Input-output Accounting Matrix (in value terms) ///
k[i] 0.137139 0.017002 0.027090 0.012532 0.308236 0.157089 0.064951 0.218803 0.567018 0.130624 0.016072 0.306593 0.016306 1[i] 0.010388 0.005512 0.007278 0.005195 0.200037 0.282357 0.022426 0.331347 0.078228 0.151829 0.249450 0.558010 0.002905
 /// 14. Social Accounting Matrix (in value terms) ///
     (0) (1) (2) (3) (4) (5) (6) (7) (0) 0.179203 -0.000055 -0.000000 -0.000000 -0.050309 -0.001459 -0.000000 -0.000062
k[i] -0.091340 -0.011324 -0.018043 -0.008347 -0.205296 -0.104627 -0.043260 -0.145731
l[i] -0.010388 -0.005512 -0.007278 -0.005195 -0.200037 -0.282357 -0.022426 -0.331347
Csum 0.000000 0.000000 0.000000 -0.000000 0.000000 -0.000000 0.000000
 \begin{pmatrix} 8 \\ 0 \\ 0 \\ -0.000000 \\ -0.000004 \\ -0.000002 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.000000 \\ -0.001490 \\ -0.001280 \\ -0.001280 \\ -0.001280 \\ -0.001280 \\ -0.00230 \\ -0.005480 \\ -0.001280 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -0.00260 \\ -
                                                                                                                                                                                         -p[i]*ES[i]
                                                                                                                                                                                         0.094642
                                                                                                                                                                                                                            0.000000
                                                                                                                                                                                         0.002318
                                                                                                                                                     -0.012649
                                                                                                                                                                                                                          -0.000000
                                                                                                                                                    -0.008739
                                                                                                                                                                                         0.002089
                                                                                                                                                                                                                            0.000000
                                                                                                                                                    -0.000215
                                                                                                                                                                                         0.002579
                                                                                                                                                                                                                          -0.000000
                                                                                                                                                    -0.640514
                                                                                                                                                                                       -0.480518
                                                                                                                                                                                                                            0.000000
                                                                                                                                                    -0.723050
                                                                                                                                                                                         0.000000
                                                                                                                                                                                                                          -0.000000
                                                                                                                                                    -0.050794
                                                                                                                                                                                       -0.025845
                                                                                                                                                                                                                            0.000000
                                                                                                                                                   -0.050794

-0.369343

-0.427477

-0.157708

-0.391494

-1.007057

-0.000234
                                                                                                                                                                                      -0.025845
0.079305
-0.016919
0.017284
0.000000
-0.269690
0.001511
                                                                                                                                                                                                                          0.000000
-0.000000
-0.000000
0.000000
                                                                                                                                                                                                                             0.000000
k[i] -0.377655 -0.087001 -0.010704 -0.204202 -0.010860 l[i] -0.078228 -0.151829 -0.299450 -0.558010 -0.002905
                                                                                                                                                      1.318389
                                                                                                                                                                                                                            0.000000
                                                                                                                                                        1.904962
                                                                                                                                                                                                                          -0.000000
                                                                                                                                                       0.593242
                                                                                                                                                                                      -0.593242
                                                                                                                                                                                                                            0.000000
-0.000000
                                                                                                                                                                                         0.000000
 /// 15. #s of iterations ///
 (15-1) Theration for general equilibrium loop: No.= 66 (15-2) The computational time: 0.001.
                                                   The end of the output file-----
```